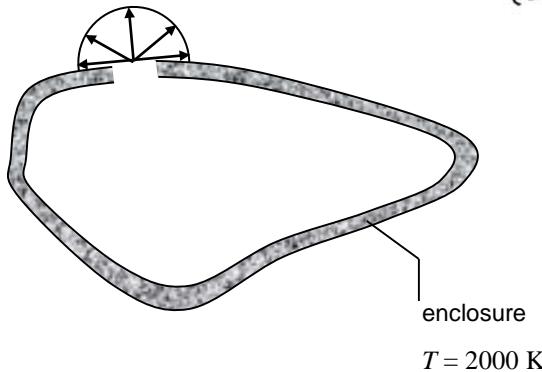


Example

Consider a large, isothermal enclosure that is maintained at a uniform temperature of 2000 K.

- Calculate the emissive power of the radiation that emerges from a small aperture on the surface.
- What is the wavelength below which 10% of the emission is concentrated?
- What is the wavelength above which 10% of the radiation is concentrated?
- Determine the maximum spectral emissive power and the wavelength at which it occurs.



$$\begin{aligned}
 (a) \quad E_b &= \sigma T^4 \\
 &= 5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \cdot \text{K}^4} \cdot (2000)^4 \text{K}^4 \\
 &= \boxed{9.07 \times 10^5 \text{ W/m}^2}
 \end{aligned}$$

$$\begin{aligned}
 (b) \quad f_{0-\lambda_1} &\approx 0.1 \quad \text{From table } \lambda_1 T \approx 2200 \mu\text{m}\cdot\text{K} \\
 \therefore \lambda_1 &= \frac{2200 \mu\text{m}\cdot\text{K}}{2000 \text{ K}} = \boxed{1.10 \mu\text{m}}
 \end{aligned}$$

$$\begin{aligned}
 (c) \quad \left. \begin{array}{l} f_{\lambda_2-\infty} = 0.1 \\ f_{0-\infty} = 1 \end{array} \right\} f_{0-\lambda_2} = 1 - f_{\lambda_2-\infty} = 1 - 0.1 = 0.9 \\
 \text{From table } \lambda_2 T = 9382 \mu\text{m}\cdot\text{K} \quad \lambda_2 = \frac{9382 \mu\text{m}\cdot\text{K}}{2000 \text{ K}} \\
 = \boxed{4.69 \mu\text{m}}
 \end{aligned}$$

(d) Wien's Displacement Law:

$$\lambda_{\text{max}} T = 2897.8 \mu\text{m}\cdot\text{K}$$

$$\lambda_{\text{max}} = \frac{2897.8 \mu\text{m}\cdot\text{K}}{2000 \text{ K}} = \boxed{1.45 \mu\text{m}}$$

$$E_{b\lambda} = \frac{c_1}{\lambda^5 \exp(c_2/\lambda T - 1)} = \frac{3.742 \times 10^8 \frac{\text{W}\cdot\mu\text{m}^4}{\text{m}^2}}{(1.45)^5 \mu\text{m}^5 \exp\left(\frac{1.439 \times 10^4 \mu\text{m}\cdot\text{K}}{2897.8 \mu\text{m}\cdot\text{K}}\right) - 1} = \boxed{4.106 \times 10^5 \frac{\text{W}}{\text{m}^2 \cdot \mu\text{m}}}$$