ROSE-HULMAN INSTITUTE OF TECHNOLOGY

ME301 – Applications of Thermodynamics

Circle section:	01 [6 th Cloutier]	02 [5 th Thom]
	03 [6 th Thom]	04 [5 th Lui]
	05 [6 th Lui]	

Exam 2

Oct 25, 2018

Rules:

- Closed book/notes exam.
- Two help sheets allowed. (8-1/2 x 11" sheet of paper, one side each, handwritten; may not contain worked out example problems)
- Maple, Excel, and MATLAB are allowed on your laptop, but nothing may be prepared before the exam.
- Either open property tables (hardcopies) or open Property Calculator Programs on your laptop.

Instructions:

- Show all work for complete credit.
- Work in symbols first, plugging in numbers and performing calculations last.

Problem 1	/ 24
Problem 2	/ 32
Problem 3	/ 44
Total	/100

СМ

Name

Problem 1 [24 points]

- (a) [6 pts] Two steam turbines with isentropic (adiabatic) efficiencies of $\eta_A = 1$ and $\eta_B = 0.85$ are considered for use in the same Rankine cycle. How would the various quantities compare for the two turbines?
 - i. Outlet specific entropies of the turbines
 - $\circ s_{out,B} < s_{out,A}$
 - $\circ \quad S_{out,B} = S_{out,A}$
 - $\circ \quad s_{out,B} > s_{out,A}$
 - ii. Outlet specific enthalpies of the turbines
 - $\circ \quad h_{out,B} < h_{out,A}$
 - $\circ \quad h_{out,B} = h_{out,A}$
 - $\circ \quad h_{out,B} > h_{out,A}$
 - iii. Outlet pressures of the turbines
 - $\circ \quad P_{out,B} < P_{out,A}$
 - $\circ \quad P_{out,B} = P_{out,A}$
 - $\circ \quad P_{out,B} > P_{out,A}$
- (b) [12 pts] A mixture of fuel and oxygen is modeled as having the following molar composition: 34% CH₄ (*M*_{CH4}=16.04) and 66% O₂ (*M*_{O2}=32). Find the <u>mass fraction of each component</u> and the <u>apparent (average) molar mass</u> of the mixture.

- (c) [6 pts] In a *cold air standard* Brayton cycle, the exit temperature of the air leaving the turbine is $T_4=200^{\circ}$ C and the temperature of the air leaving the compressor is $T_2=100^{\circ}$ C.
 - i. If the cycle makes use of an ideal regenerator, the temperature of the air entering the high pressure heat exchanger will be
 - \circ $T_x = 100^{\circ}C$
 - $100^{\circ}C < T_x < 200^{\circ}C$
 - \circ $T_x = 200^{\circ}C$
 - ii. If the cycle makes use of an non-ideal regenerator, the temperature of the air entering the high pressure heat exchanger will be
 - \circ $T_x = 100^{\circ}C$
 - $100^{\circ}C < T_x < 200^{\circ}C$
 - \circ $T_x = 200^{\circ}C$
 - iii. If the cycle is instead an *air-standard* Brayton cycle (not cold air standard), ideal regeneration would result in
 - \circ $T_x = 100^{\circ}C$
 - $100^{\circ}C < T_x < 200^{\circ}C$
 - \circ $T_x = 200^{\circ}C$

Problem 2 [32 points]

1.5 kmol/s of gaseous oxygen at 350 K and 200 kPa is mixed with 3.5 kmol/s of gaseous nitrogen at 350 K and 200 kPa. The mixture stream is then throttled to standard room pressure at 100 kPa through a valve.



- (a) If the process is *adiabatic*, determine the <u>mixture temperature at the exit</u>.
- (b) Determine the entropy generation rate during the mixing-throttling process, in kW/K.

Clearly document your solution for full credit.

Problem 3 [44 points]

A piston-cylinder operates on the Worst-Efficiency-Ever Cycle (WEEC) with steam as the working fluid. The cycle consists of the following three processes:

> State (1) to (2): Constant volume heat addition State (2) to (3): Reversible, adiabatic expansion State (3) to (1): Constant pressure heat rejection

At the beginning of the heat addition process, 0.1 kg of water exists as a saturated vapor at 100 kPa.

- (a) Find the maximum cycle temperature.
- (b) Fill in the table with the <u>work and heat transfer associated</u> with each requested process. (Note: show all work for full credit.)
- (c) Calculate the <u>cycle efficiency</u>.



v [m³/kg]



Process	W(kJ)	Q (kJ)
$(1) \rightarrow (2)$		27.29
$(2) \rightarrow (3)$		
$(3) \rightarrow (1)$		



s [kJ/kg-K]

<u>Length</u>

1 ft = 12 in = 0.3048 m = 1/3 yd 1 m = 100 cm = 1000 mm = 39.37 in = 3.2808 ft 1 mile = 5280 ft = 1609.3 m

Mass

1 kg = 1000 g = 2.2046 lbm 1 lbm = 16 oz = 0.45359 kg 1 slug = 32.174 lbm

Temperature Values

 $\begin{array}{l} (T/K) = (T/ \circ R) / 1.8 \\ (T/K) = (T/ \circ C) + 273.15 \\ (T/ \circ C) = [(T/ \circ F) - 32] / 1.8 \\ (T/ \circ R) = 1.8 (T/K) \\ (T/ \circ R) = (T/ \circ F) + 459.67 \\ (T/ \circ F) = 1.8 (T/ \circ C) + 32 \end{array}$

Temperature Differences

 $(\Delta T/^{\circ} R) = 1.8(\Delta T/K)$ $(\Delta T/^{\circ} R) = (\Delta T/^{\circ} F)$ $(\Delta T/K) = (\Delta T/^{\circ} C)$

<u>Volume</u>

 $1 m^{3} = 1000 L = 10^{6} cm^{3} = 10^{6} mL = 35.315 ft^{3}$ = 264.17 gal $1 ft^{3} = 1728 in^{3} = 7.4805 gal = 0.028317 m^{3}$ $1 gal = 0.13368 ft^{3} = 0.0037854 m^{3}$

Volumetric Flow Rate

1 m³/s = 35.315 ft³/s = 264.17 gal/s 1 ft³/s = 1.6990 m³/min = 7.4805 gal/s = 448.83 gal/min

Force

 $1 N = 1 kg m/s^{2} = 0.22481 lbf$ $1 lbf = 1 slug ft/s^{2} = 32.174 lbm ft/s^{2}$ = 4.4482 N

Pressure

1 atm = 101.325 kPa = 1.01325 bar = 14.696 lbf/in² 1 bar = 100 kPa = 10⁵ Pa 1 Pa = 1 N/m² = 10⁻³ kPa 1 lbf/in² = 6.8947 kPa = 6894.7 N/m²; [lbf/in² = "psi"]

Energy

 $\begin{array}{l} 1 \ J \ = \ 1 \ N \ m \\ 1 \ J \ = \ 1 \ Pa \ m^3 \\ 1 \ kJ \ = \ 1000 \ J \ = \ 737.56 \ ft \ lbf \ = \ 0.94782 \ Btu \\ 1 \ Btu \ = \ 1.0551 \ kJ \ = \ 778.17 \ ft \ lbf \\ 1 \ ft \ lbf \ = \ 1.3558 \ J \end{array}$

Energy Transfer Rate

1 kW = 1 kJ/s = 737.56 ft ·lbf/s = 1.3410 hp = 0.94782 Btu/s 1 Btu/s = 1.0551 kW = 1.4149 hp = 778.17 ft ·lbf/s 1 hp = 550 ft ·lbf/s = 0.74571 kW = 0.70679 Btu/s

Specific Energy

1 kJ/kg = 1000 m²/s² 1 Btu/lbm = 25037 ft²/s² 1 ft·lbf /lbm = 32.174 ft²/s²

Other useful information	SI	USCS
Universal Ideal Gas Constant: \bar{R}	= 8.314 kJ/(kmol-K)	= 1545 (ft-lbf)/(lbmol-R)
		= 1.986 Btu/(lbmol-R)
Acceleration of Gravity: g	$= 9.810 \text{ m/s}^2$	$= 32.174 \text{ ft/s}^2$