

NAME _____

SECTION _____

BOX NUMBER _____

Problem 1 (30) _____

Problem 2 (30) _____

Problem 3 (40) _____

Total (100) _____

INSTRUCTIONS

- Closed book/notes exam. (Unit conversion page provided)
- Help sheet allowed. (8-1/2 x 11" sheet of paper, one side)
- Laptops may be used; however, no pre-prepared worksheets or files may be used.
- Doing a handstand on the table while your classmates rock it back and forth will result in a standing ovation, but unfortunately no extra points.

1) Show all work for complete credit.

- Start all problems at the ANALYSIS stage, but clearly label any information you use for your solution.

• **Problems involving conservation principles MUST CLEARLY IDENTIFY THE SYSTEM IN A SEPARATE DRAWING and show a clear, logical progression from the basic principle.**

- Don't expect us to read your mind as to how or why you did something in the solution. Clearly indicate how you arrived at your answer.
- **Always crunch numbers last on an exam.** The final numerical answer is worth the least amount of points. (Especially if all I would have to do is plug in the numbers into a well-documented solution.)

2) Useful Rule of Thumb (Heuristic): (100 point exam)/(50 min) = 2 points/minute. That means a 10 point problem is not worth more than 5 minutes of your time (at least the first time around).

3) Please remain seated until the end of class or everyone finishes. (Raise your hand and I'll pick up your exam if you have other work you need or want to do.)

<u>USEFUL INFORMATION</u>	SI	USCS	Molar Mass	
Ideal Gas Constant: R_u	= 8.314 kJ/(kmol-K)	= 1545 (ft-lbf)/(lbmol-°R)	Air	28.97
		= 1.986 Btu/(lbmol-°R)	O ₂	32.00
Standard Acceleration of Gravity: g	= 9.810 m/s ²	= 32.174 ft/s ²	N ₂	28.01
Density of liquid water	= 1000 kg/m ³	= 62.4 lbm/ft ³	H ₂	2.016
		= 1.94 slug/ft ³	CO ₂	44.01

Problem 1 (30 pts)

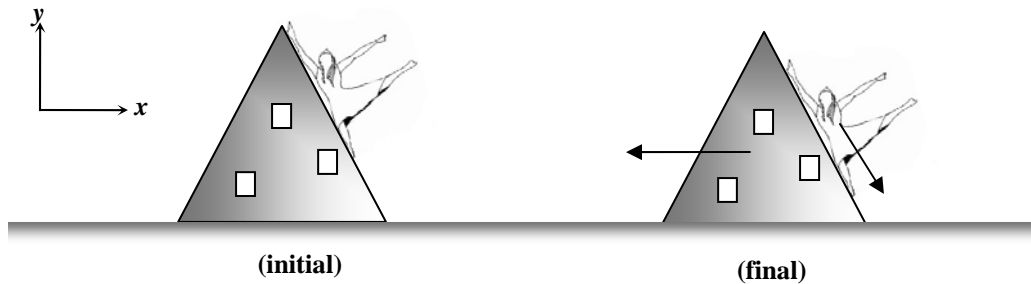
Answer each of the following unrelated questions.

- a) (5 pts) A Diavolo dancer is on a pyramid. Initially both the dancer and the pyramid are at rest. The dancer then slides down pyramid, causing it to slide across the stage in the opposite direction. If all surfaces are frictionless, the x-direction momentum of a system consisting of dancer and pyramid combined

i. increases

ii. decreases

iii. remains constant



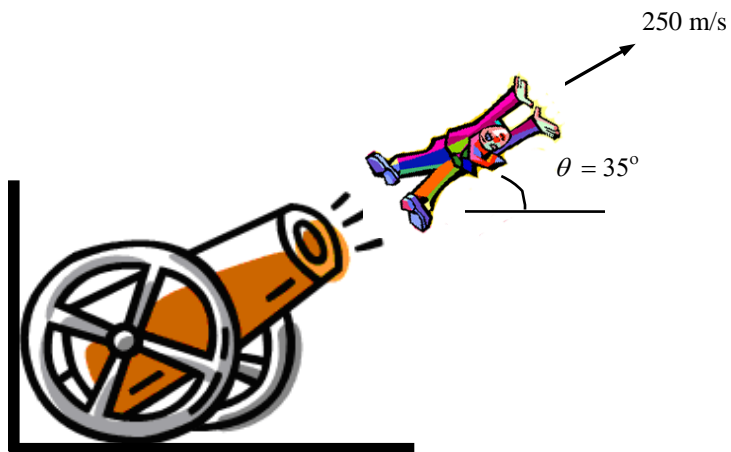
- b) (5 pts) If there is kinetic friction between the pyramid and the stage for a) above, the x-direction momentum of a system consisting of dancer and pyramid combined

i. increases

ii. decreases

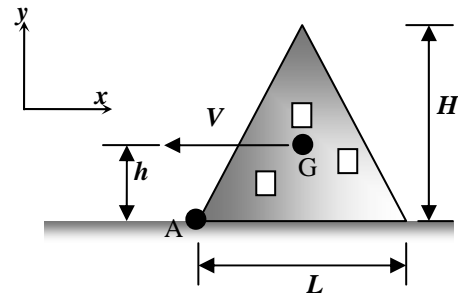
iii. remains constant

- c) (7 pts) A young 40-kg Diavolo acrobat is launched by a 300-kg cannon at a speed of 250 m/s and an angle of 35° with respect to the horizontal. Determine the impulse exerted by the ground and the vertical wall on the cannon during the launching process.

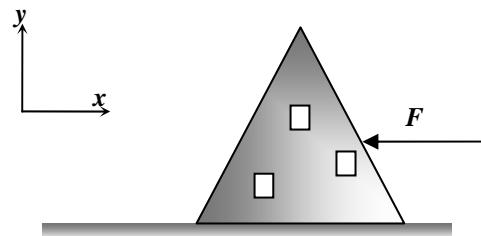


d) (5 pts) The Diavolo pyramid below is moving to the left at a velocity V . The angular velocity of the block about point A is

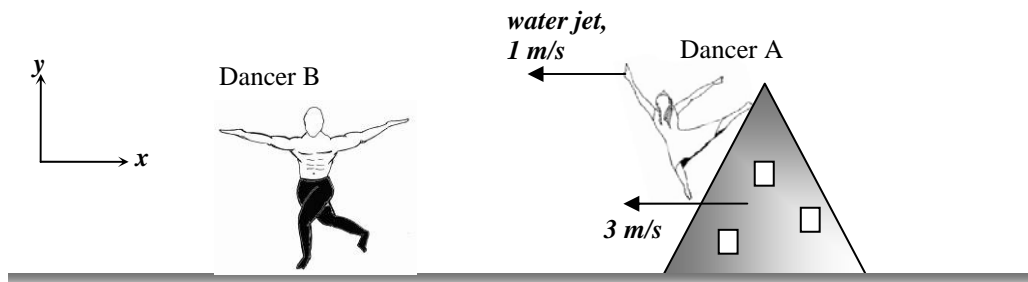
- i. mHV cw ii. mHV ccw
- iii. mhV cw iv. mhV ccw
- v. mLV cw vi. mLV ccw
- vii. 0 viii. None of the above



e) (4 pts) This Diavolo pyramid is not moving. It has a mass m , and the coefficients of static and kinetic friction between the pyramid and the ground are μ_k and μ_s , respectively. A force F is applied to the pyramid. What is the friction force exerted on the pyramid by the ground? (Indicate magnitude and direction.)



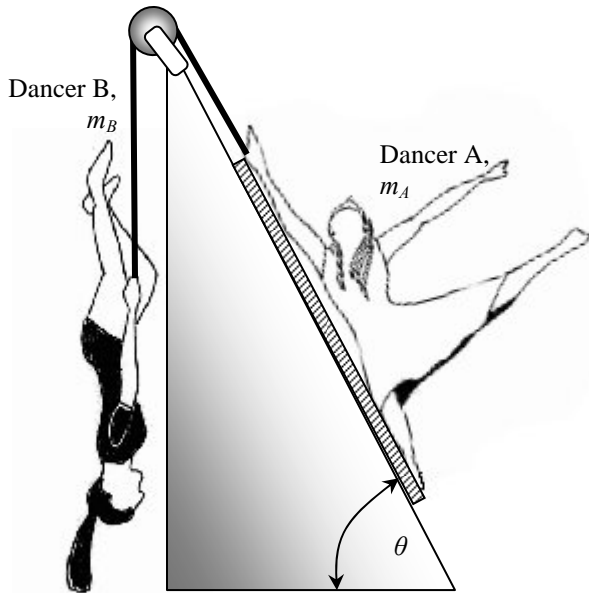
f) (4 pts) Dancer A rides a pyramid to the left at a velocity of 3 m/s. She squirts water, with a velocity relative to the platform of 1 m/s, at stationary Dancer B. What is the water velocity observed by Dancer B, i.e. what is the velocity of the water with respect to the ground?



- i) 4 m/s to the left ii) 3 m/s to the left iii) 2 m/s to the left iv) 1 m/s to the left v) None of these

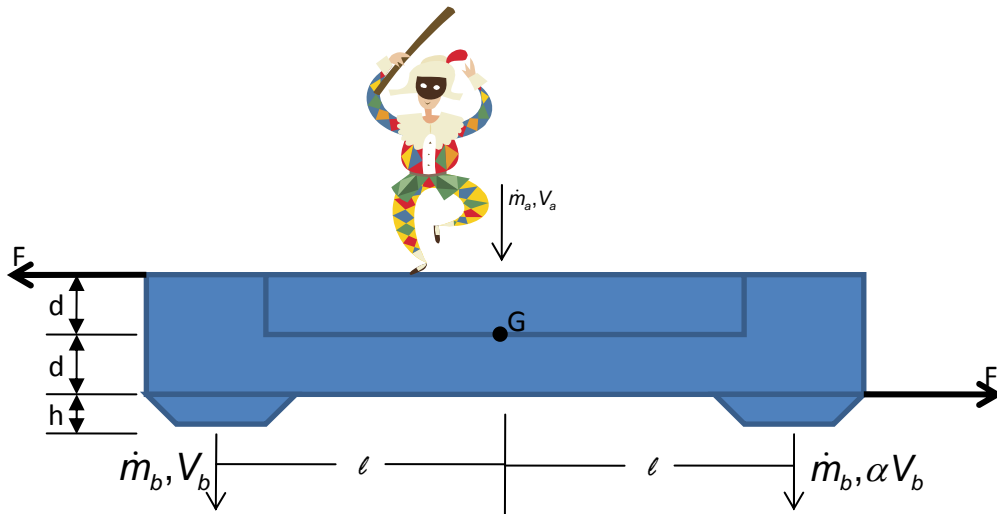
Problem 2 (30 pts)

In a new Diavolo piece, a dancer with mass m_A rides a sled upward on an incline of angle θ while another dancer with mass m_B descends toward the stage hanging upside down on a rope as shown in the figure. Dancer A and Dancer B are joined by an inextensible cord which is wrapped around a massless and frictionless pulley. The coefficient of friction between dancer A's sled and the incline is μ_k . Assuming both dancers are initially at rest, find the necessary equations to find the acceleration of each dancer and the tension in the rope. **YOU DO NOT HAVE TO SOLVE THE EQUATIONS.** Clearly label the equations to be solved and list the unknowns.



Problem 3 (40 pts)

You have been hired to build a stationary hovering dancing platform for Diavolo. This platform consists of a large intake fan which draws air in with a flow rate of \dot{m}_A . This air is split evenly to two (2) fans below the platform such that **the outlet velocity of the front fan is proportional to the outlet velocity of the rear fan**, although the two mass flow rates are the same. Two other dancers apply equal forces to two ropes used to hold the platform at the correct locations on the stage. The cart and dancer have a combined mass of m_{cart} with a center of gravity at point G. Assume that F , \dot{m}_A , V_a , m_{cart} , g , ℓ , h , and d are known. We wish to find the remaining parameters (α , V_b , \dot{m}_B) so that the platform remains level and floats at a constant height above the stage. **SET UP THE EQUATIONS BUT DO NOT SOLVE THEM. Clearly label the equations to be solved and list the unknowns.**



Length

$$1 \text{ ft} = 12 \text{ in} = 0.3048 \text{ m} = 1/3 \text{ yd}$$

$$1 \text{ m} = 100 \text{ cm} = 1000 \text{ mm} = 39.37 \text{ in} = 3.2808 \text{ ft}$$

$$1 \text{ mile} = 5280 \text{ ft} = 1609.3 \text{ m}$$

Mass

$$1 \text{ kg} = 1000 \text{ g} = 2.2046 \text{ lbm}$$

$$1 \text{ lbm} = 16 \text{ oz} = 0.45359 \text{ kg}$$

$$1 \text{ slug} = 32.174 \text{ lbm}$$

Temperature Values

$$(T/\text{K}) = (T/^{\circ}\text{R}) / 1.8$$

$$(T/\text{K}) = (T/^{\circ}\text{C}) + 273.15$$

$$(T/^{\circ}\text{C}) = [(T/^{\circ}\text{F}) - 32] / 1.8$$

$$(T/^{\circ}\text{R}) = 1.8(T/\text{K})$$

$$(T/^{\circ}\text{R}) = (T/^{\circ}\text{F}) + 459.67$$

$$(T/^{\circ}\text{F}) = 1.8(T/^{\circ}\text{C}) + 32$$

Temperature Differences

$$(\Delta T/^{\circ}\text{R}) = 1.8(\Delta T/\text{K})$$

$$(\Delta T/^{\circ}\text{R}) = (\Delta T/^{\circ}\text{F})$$

$$(\Delta T/\text{K}) = (\Delta T/^{\circ}\text{C})$$

Volume

$$1 \text{ m}^3 = 1000 \text{ L} = 10^6 \text{ cm}^3 = 10^6 \text{ mL} = 35.315 \text{ ft}^3$$

$$= 264.17 \text{ gal}$$

$$1 \text{ ft}^3 = 1728 \text{ in}^3 = 7.4805 \text{ gal} = 0.028317 \text{ m}^3$$

$$1 \text{ gal} = 0.13368 \text{ ft}^3 = 0.0037854 \text{ m}^3$$

Volumetric Flow Rate

$$1 \text{ m}^3/\text{s} = 35.315 \text{ ft}^3/\text{s} = 264.17 \text{ gal/s}$$

$$1 \text{ ft}^3/\text{s} = 1.6990 \text{ m}^3/\text{min} = 7.4805 \text{ gal/s} = 448.83 \text{ gal/min}$$

Force

$$1 \text{ N} = 1 \text{ kg}\cdot\text{m}/\text{s}^2 = 0.22481 \text{ lbf}$$

$$1 \text{ lbf} = 1 \text{ slug}\cdot\text{ft}/\text{s}^2 = 32.174 \text{ lbm}\cdot\text{ft}/\text{s}^2 = 4.4482 \text{ N}$$

Pressure

$$1 \text{ atm} = 101.325 \text{ kPa} = 1.01325 \text{ bar} = 14.696 \text{ lbf}/\text{in}^2$$

$$1 \text{ bar} = 100 \text{ kPa} = 10^5 \text{ Pa}$$

$$1 \text{ Pa} = 1 \text{ N}/\text{m}^2 = 10^{-3} \text{ kPa}$$

$$1 \text{ lbf}/\text{in}^2 = 6.8947 \text{ kPa} = 6894.7 \text{ N}/\text{m}^2$$

[lbf/in² often abbreviated as "psi"]

Energy

$$1 \text{ J} = 1 \text{ N}\cdot\text{m}$$

$$1 \text{ kJ} = 1000 \text{ J} = 737.56 \text{ ft}\cdot\text{lbf} = 0.94782 \text{ Btu}$$

$$1 \text{ Btu} = 1.0551 \text{ kJ} = 778.17 \text{ ft}\cdot\text{lbf}$$

$$1 \text{ ft}\cdot\text{lbf} = 1.3558 \text{ J}$$

Energy Transfer Rate

$$1 \text{ kW} = 1 \text{ kJ}/\text{s} = 737.56 \text{ ft}\cdot\text{lbf}/\text{s} = 1.3410 \text{ hp} = 0.94782 \text{ Btu}/\text{s}$$

$$1 \text{ Btu}/\text{s} = 1.0551 \text{ kW} = 1.4149 \text{ hp} = 778.17 \text{ ft}\cdot\text{lbf}/\text{s}$$

$$1 \text{ hp} = 550 \text{ ft}\cdot\text{lbf}/\text{s} = 0.74571 \text{ kW} = 0.70679 \text{ Btu}/\text{s}$$

Specific Energy

$$1 \text{ kJ}/\text{kg} = 1000 \text{ m}^2/\text{s}^2$$

$$1 \text{ Btu}/\text{lbm} = 25037 \text{ ft}^2/\text{s}^2$$

$$1 \text{ ft}\cdot\text{lbf} / \text{lbm} = 32.174 \text{ ft}^2/\text{s}^2$$