

# Conservation of linear momentum

$$\frac{d}{dt}(\bar{P}_{sys}) = \sum \bar{F} + \sum_{in} \dot{m} \bar{V} - \sum_{out} \dot{m} \bar{V}$$

1) A closer look at  $\vec{P}_{sys}$

a. System is a **particle**

$$\vec{P}_{sys} = m_{sys} \vec{V}_{sys}$$

b. System has **uniform velocity**

$$\vec{P}_{sys} = m_{sys} \vec{V}_{sys}$$

c. System is a **general closed system**

$$\vec{P}_{sys} = \int_{\nabla_{sys}} \vec{V} \rho d\nabla$$

$$\text{Let } \vec{V}_G = \frac{d\vec{r}_G}{dt}$$

$$\text{where } \vec{r}_G = \frac{1}{m_{sys}} \int_{\nabla_{sys}} \vec{r} \rho d\nabla$$

Then  $\vec{P}_{sys} = m_{sys} \vec{V}_G$

**Velocity at center of mass**

2) A closer look at  $F$  (Rate of LM transport at non-flow boundaries)

a. **Body forces** (“Forces at a distance”)

- Drawn at: “Center of mass/charge/etc.”
- E.g., gravity, electrostatic...
- Act on **whole body**, but we pretend they act at a point

No contact is needed, but the forces still cross system boundary!

b. **Contact forces** (Come from interaction between bodies in contact.)

Drawn at: boundaries where things touch each other

c. **Contact stresses**

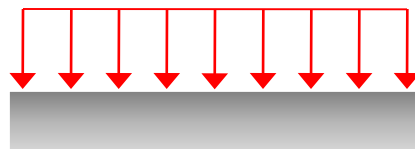
i. Shear

$$= F_{tan}/Area$$



ii. Normal

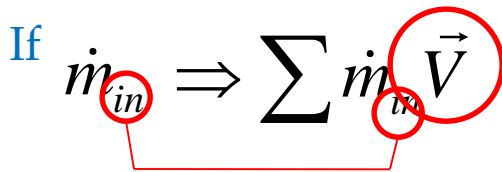
$$= F_{normal}/Area$$



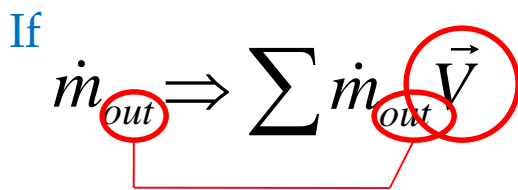
E.g., pressure!

3) A closer look at  $\dot{m}\vec{V}$  (Rate of LM transport at flow boundaries)

If  $\dot{m}_{in} \Rightarrow \sum \dot{m}_{in} \vec{V}$



If  $\dot{m}_{out} \Rightarrow \sum \dot{m}_{out} \vec{V}$



These are *vectors*. Thus they have signs in the component equations and can make entire term *positive or negative*.