

Problem 16.158

The uniform rod AB of weight W is released from rest when

$$\beta = 70^\circ.$$

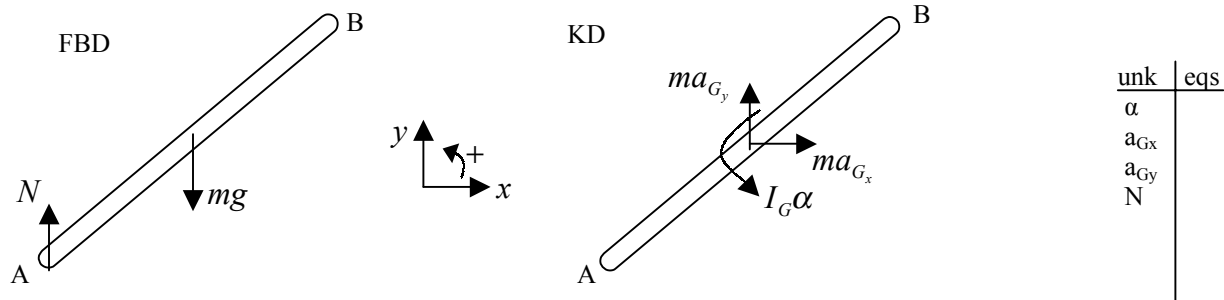
Assuming the friction force is zero between end A and the surface, determine immediately after release

- a) the angular acceleration of the mass center of the rod
- b) the acceleration of the mass center of the rod
- c) the reaction at A

Step 1 : Identify System: *The Rod*

Step 2 : Identify Form of Equations Required: *need acceleration and force, therefore use Rate Form*

Step 3 : Draw system diagrams according to choice of equation form and identify unknowns : *FBD and KD*



Step 4 : Kinetics

COLM(RF) in x-dir $0 = ma_{G_x}$ (1)

COLM(RF) in y-dir $N - mg = ma_{G_y}$ (2)

COAM(RF) about point G $-N \frac{l}{2} \cos(70^\circ) = I_G \alpha$ (3)

Step 5 : Kinematics

Relative acceleration of G wrt A

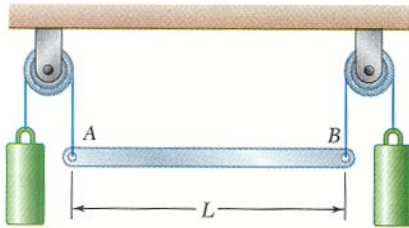
$$\begin{aligned} \bar{a}_G &= \bar{a}_A + \bar{a}_{G/A} \\ &= \bar{a}_A + \bar{\alpha} \times \bar{r}_{G/A} - \omega^2 \bar{r}_{G/A} \\ &= a_{A_x} \hat{i} + a_{A_y} \hat{j} + (\alpha \hat{k}) \times \left(\frac{l}{2} \cos(70^\circ) \hat{i} + \frac{l}{2} \sin(70^\circ) \hat{j} \right) - 0 \end{aligned}$$

Collecting i and j components ($a_{A_y}=0!$)

i components $a_{G_x} = a_{A_x} - \frac{l}{2} \cos(70^\circ) \alpha$ (4)

j components $a_{G_y} = a_{A_y} + \frac{l}{2} \sin(70^\circ) \alpha$ (5)

Step 6: Solve in Maple



Problem 16.160

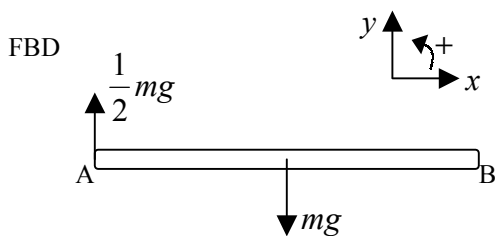
The slender rod AB of weight W is held in equilibrium by two counterweights each of mass $1/2W$. If the wire at B is cut, determine the acceleration at that instant

- a) of point A
- b) of point B

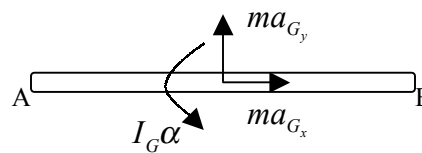
Step 1 : Identify System: *The Rod*

Step 2 : Identify Form of Equations Required: *need acceleration and force, therefore use Rate Form*

Step 3 : Draw system diagrams according to choice of equation form **and identify unknowns** : *FBD and KD*



KD



unk	eqs
a_{Ax}	
a_{Ay}	
a_{Bx}	
a_{By}	
a_{Gx}	
a_{Gy}	
α	

Step 4 : Kinetics

COLM(RF) in x-dir $0 = ma_{G_x}$ (1)

COLM(RF) in y-dir $\frac{1}{2}mg - mg = ma_{G_y}$ (2)

COAM(RF) about point G $-\frac{1}{2}mg \frac{l}{2} = I_G \alpha$ (3)

Step 5 : Kinematics

Relative acceleration of A wrt G

$$\begin{aligned} \bar{a}_A &= \bar{a}_G + \bar{a}_{A/G} \\ &= \bar{a}_G + \bar{\alpha} \times \bar{r}_{A/G} - \omega^2 \bar{r}_{A/G} \\ &= a_{G_x} \hat{i} + a_{G_y} \hat{j} + (\alpha \hat{k}) \times \left(-\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0 \end{aligned}$$

Collecting i and j components

i components $a_{A_x} = a_{G_x}$ (4)

j components $a_{A_y} = a_{G_y} - \alpha \frac{l}{2}$ (5)

Relative motion of B wrt G

$$\begin{aligned}\bar{a}_B &= \bar{a}_G + \bar{a}_{B/G} \\ &= \bar{a}_G + \bar{\alpha} \times \bar{r}_{B/G} - \omega^2 \bar{r}_{B/G} \\ &= a_{G_x} \hat{i} + a_{G_y} \hat{j} + (\alpha \hat{k}) \times \left(\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0\end{aligned}$$

Collecting i and j components

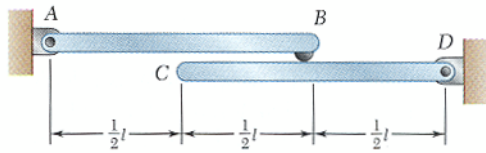
i components

$$a_{B_x} = a_{G_x} \quad (6)$$

j components

$$a_{B_y} = a_{G_y} + \alpha \frac{l}{2} \quad (7)$$

Step 6: Solve in Maple



Problem 16.162

Two slender rods of length l and mass m , are released from rest in the positions shown. Knowing that a small knob at end B of rod AB bears on rod CD, determine immediately after release

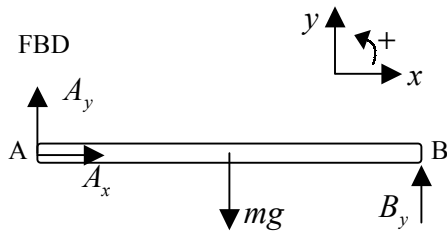
- a) the acceleration of end C of the rod CD
- b) the force exerted on the knob

Step 1 : Identify System: Both Rod

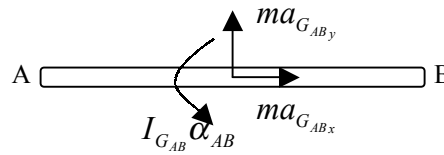
Step 2 : Identify Form of Equations Required: need acceleration and force, therefore use Rate Form

Step 3 : Draw system diagrams according to choice of equation form and identify unknowns : FBD and KD

Rod AB

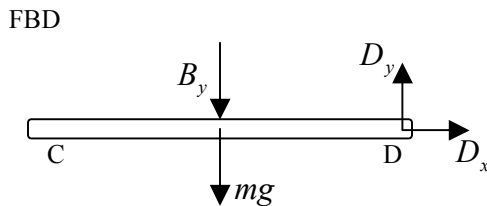


KD

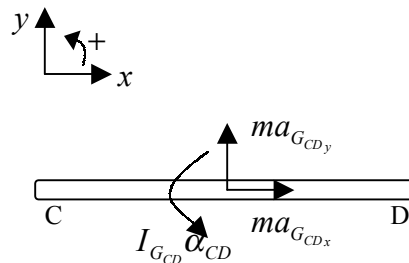


unk	eqs
a_{Cx}	
a_{Cy}	
B_y	
A_x	
A_y	
D_x	
D_y	
a_{GABx}	
a_{GABy}	
α_{AB}	
a_{GCDx}	
a_{GCDy}	
α_{CD}	

Rod BC



KD



Step 4 : Kinetics

Rod AB

COLM(RF) in x-dir $A_x = ma_{G_{ABx}}$ (1)

COLM(RF) in y-dir $A_y + B_y - mg = ma_{G_{ABy}}$ (2)

COAM(RF) about point G $-A_y \frac{l}{2} + B_y \frac{l}{2} = I_{G_{AB}} \alpha_{AB}$ (3)

Rod CD

COLM(RF) in x-dir $D_x = ma_{G_{CDx}}$ (4)

COLM(RF) in y-dir $D_y - B_y - mg = ma_{G_{CDy}}$ (5)

COAM(RF) about point G $D_y \frac{l}{2} = I_{G_{CD}} \alpha_{CD}$ (6)

Step 5 : Kinematics

Rod AB

Relative acceleration of G wrt A

$$\begin{aligned}\bar{a}_G &= \bar{a}_A + \bar{a}_{G/A} \\ &= \bar{a}_A + \bar{\alpha}_{AB} \times \bar{r}_{G/A} - \omega_{AB}^2 \bar{r}_{G/A} \\ &= 0 + (\alpha_{AB} \hat{k}) \times \left(\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0\end{aligned}$$

Collecting i and j components

$$\text{i components} \quad a_{G_{ABx}} = 0 \quad (7)$$

$$\text{j components} \quad a_{G_{ABy}} = \alpha \frac{l}{2} \quad (8)$$

Rod CD

Relative acceleration of G wrt D

$$\begin{aligned}\bar{a}_G &= \bar{a}_D + \bar{a}_{G/D} \\ &= \bar{a}_D + \bar{\alpha}_D \times \bar{r}_{G/D} - \omega_{CD}^2 \bar{r}_{G/D} \\ &= 0 + (\alpha_{CD} \hat{k}) \times \left(-\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0\end{aligned}$$

Collecting i and j components

$$\text{i components} \quad a_{G_{CDx}} = 0 \quad (9)$$

$$\text{j components} \quad a_{G_{CDy}} = -\alpha \frac{l}{2} \quad (10)$$

Relative acceleration of C wrt G

$$\begin{aligned}\bar{a}_C &= \bar{a}_G + \bar{a}_{C/G} \\ &= \bar{a}_G + \bar{\alpha}_{CD} \times \bar{r}_{C/G} - \omega_{CD}^2 \bar{r}_{C/G} \\ &= (a_{G_{CDx}} \hat{i} + a_{G_{CDy}} \hat{j}) + (\alpha_{CD} \hat{k}) \times \left(-\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0\end{aligned}$$

Collecting i and j components

$$\text{i components} \quad a_{C_x} = a_{G_{CDx}} \quad (11)$$

$$\text{j components} \quad a_{C_y} = a_{G_{CDy}} - \alpha_{CD} \frac{l}{2} \quad (12)$$

Need one more equation ...

Relating point B - the acceleration of point B must be the same on both rods

Rod AB

Relative acceleration of B wrt G

$$\begin{aligned}\bar{a}_B &= \bar{a}_G + \bar{a}_{B/G} \\ &= \bar{a}_G + \bar{\alpha}_{AB} \times \bar{r}_{B/G} - \omega_{AB}^2 \bar{r}_{B/G} \\ &= a_{G_{ABx}} \hat{i} + a_{G_{ABy}} \hat{j} + (\alpha_{AB} \hat{k}) \times \left(\frac{l}{2} \hat{i} + 0 \hat{j} \right) - 0\end{aligned}$$

Collecting i and j components

$$\text{i components} \quad a_{B_x} = a_{G_{ABx}} \quad (13)$$

$$\text{j components} \quad a_{B_y} = a_{G_{ABy}} + \alpha_{AB} \frac{l}{2} \quad (14)$$

Rod CD

Relative acceleration of B wrt G

$$\begin{aligned}\bar{a}_B &= \bar{a}_G + \bar{a}_{B/G} \\ &= \bar{a}_G + \bar{\alpha}_{CD} \times \bar{r}_{B/G} - \omega_{CD}^2 \bar{r}_{B/G} \\ &= (a_{G_{CDx}} \hat{i} + a_{G_{CDy}} \hat{j}) + 0 - 0\end{aligned}$$

Collecting i and j components

$$\text{i components} \quad a_{B_x} = a_{G_{CDx}} \quad (15)$$

$$\text{j components} \quad a_{B_y} = a_{G_{CDy}} \quad (16)$$

Step 6: Solve in Maple