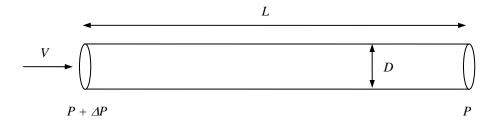
Supplementary Homework Problem (HW Set 20)

Due at the beginning of Lecture 22

Dimensional analysis of pipe friction

Consider a fluid flow through the a horizontal, circular pipe:



The pressure drop, from the inlet to the outlet, due to friction in the pipe, ΔP , depends on the following fluid properties and geometry parameters:

- a) fluid density, ρ
- b) flow velocity, V
- c) pipe diameter, D
- d) fluid viscosity, μ
- e) pipe surface roughness, ε
- f) pipe length, L

In dimensional form, the dependency can be expressed as

$$\Delta P = f(\rho, V, D, \mu, \varepsilon, L)$$
.

Perform a dimensional analysis on the above functional dependency by choosing the <u>fluid density</u>, the <u>flow velocity</u> and the <u>pipe diameter</u> as the repeating variables.

What are $\Pi_1, \Pi_2, \Pi_3, ...$ in the equivalent non-dimensional representation?

$$\Pi_1 = g(\Pi_2, \Pi_3, \ldots).$$