

ECE-320: Linear Control Systems
Homework 10

Due: Tuesday November 8 at 2 PM

1) Consider the following characteristic equations

$$\Delta(s) = s^2 + bs + 1$$

$$\Delta(s) = s^3 + bs^2 + cs + 1$$

$$\Delta(s) = s^4 + bs^3 + cs^2 + ds + 1$$

- a) Show that for the 2nd order system we need $b > 0$ for no RHP poles
- b) Show that for the 3rd order system we need $b > 0$, $c > 0$, and $bc - 1 > 0$ for no RHP poles
- c) Show that for the 4th order system we need $b > 0$, $c > 0$, $d > 0$ and $bcd - d^2 - b^2 > 0$ for no RHP poles

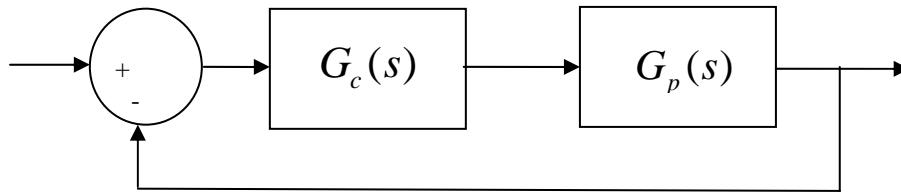
2) For $\Delta(s) = s^3 + s^2 + 2s + 2$,

- a) determine if there are any poles in the RHP
- b) if possible factor the characteristic equation and determine all of the poles

3) For $\Delta(s) = s^4 + 2s^3 + 4s^2 + 6s + 3$,

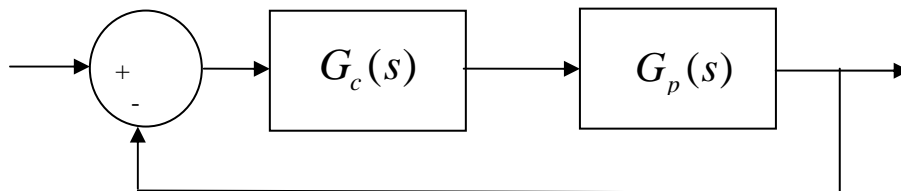
- a) determine if there are any poles in the RHP
- b) if possible factor the characteristic equation and determine all of the poles

4) Consider the following control system with plant $G_p(s) = \frac{1}{s^2 + s + 1}$



- a) For the integral controller $G_c(s) = \frac{k}{s}$, use the Routh array to show that there are no poles in the RHP for $0 < k < 1$. Verify your results using Matlab (either *sisotool* or the *rlocus* command).
- b) For the PI controller $G_c(s) = \frac{k(s+z)}{s}$, with $z > 0$, show that for no RHP poles we must have $z < 1$ and $k > 0$, or for $z > 1$ we must have $0 < k < \frac{1}{z-1}$. Determine the factors of $\Delta(s)$. Verify your results using Matlab (either *sisotool* or the *rlocus* command).

5) Consider the following control system with plant $G_p(s) = \frac{1}{s^2 + 2s + 1}$



- a) For the integral controller $G_c(s) = \frac{k}{s}$, use the Routh array to show that there are no poles in the RHP for $0 < k < 2$. Verify your results using Matlab (either *sisotool* or the *rlocus* command).
- b) For the PI controller $G_c(s) = \frac{k(s+z)}{s}$, with $z > 0$, show that for no RHP poles we must have $0 < z < 2$ and $k > 0$, or for $z > 2$ we must have $0 < k < \frac{2}{z-2}$. Determine the factors of $\Delta(s)$. Verify your results using Matlab (either *sisotool* or the *rlocus* command).