MA/CSSE 473 – Design and Analysis of Algorithms

Homework 3 48 points total

Turn this in to the HW 03 drop box on ANGEL.

When a problem is given by number, it is from the textbook. 1.1.2 means "problem 2 from section 1.1".

Problems for enlightenment/practice/review (not to turn in, but you should think about them):

How many of them you need to do serious work on depends on you and your background. I do not want to make everyone do one of them for the sake of the (possibly) few who need it. You can hopefully figure out which ones you need to do.

- 3.1.5 (selection sort practice)
- 3.1.10 (Is bubble sort stable?)

Problems to write up and turn in:

1. (5) Prove by mathematical induction that the following formula is true for every positive integer n.

$$\sum_{i=1}^{n} (-1)^{i+1} i^2 = \frac{(-1)^{n+1} n(n+1)}{2}$$

2. (8) Prove (not necessarily directly by mathematical induction) that $\sum_{i=1}^{n} i \cdot r^{i} < \frac{r}{(1-r)^{2}}$ for all $n \ge 1$ and 0 < r < 1.

3. (4) Let F_n be the nth Fibonacci number (recall that $F_0 = 0$ and $F_1 = 1$ in our formulation). Show by mathematical induction that that for all n> 0,

$$\sum_{i=1}^{n} F_{i}^{2} = F_{n} F_{n+1}$$

- (8) Prove by mathematical induction that F_n (as defined above) is even if and only if n is divisible by 3. Be sure to show both directions.
- 5. (4) 3.1.2 (algorithms for computing a^n)
- 6. (7) 3.1.4 (polynomial evaluation)
- 7. (2) 3.1.6 (stability of selection sort)
- 8. (2) 3.1.7 (selection sort linked list)
- 9. (8) 3.1.11 (alternating disks) Come up with the best solution that you can, and come up with a formula for the number of moves as a function of N, the total number of disks. Show how you get your formula. You may assume that N is even.