

# MA/CSSE 473 – Design and Analysis of Algorithms

## Homework 2 – 50 points

These are to be turned in to a drop box on ANGEL. You may write your solutions by hand and scan them if you wish. There is an easy-to-use network scanner in F-217. It will email the scan to you.

When a problem is listed by number, it is from the textbook (Levitin, 2<sup>nd</sup> edition).

1.1.2 means “problem 2 from section 1.1” .

### Problems for enlightenment/practice/review (not to turn in, but you should think about them):

How many of them you need to do serious work on depends on you and your background. I do not want to make everyone do one of them for the sake of the (possibly) few who need it. You can hopefully figure out which ones you need to do.

- 2.1.7 (and 2.1.8. Effect of changing problem size on runtime)
- 2.1.10 (chess-board doubling)
- 2.2.1 (efficiency of sequential search)
- 2.2.2 (informal definitions of asymptotic notations)
- 2.2.6 (orders of growth for polynomials and exponentials)
- 2.2.9 (effect of presorting on running time)
- 2.3.1 (summation practice)
- 2.3.5 (Secret algorithm)
- 2.3.6 (Enigma algorithm)

Another good practice problem to prepare for this assignment: The “growable array” exercise from 230. See the three files from days 01 and 02 in the [230-materials folder](#).

### Problems to write up and turn in:

1. 2.1.4 (6 points) (socks and gloves)
2. 2.1.5 (6 points) (number of digits in the representation of a positive integer)
3. 2.2.3 (10 points) (big-theta of specific functions with proofs)  
For parts a&b, use limits;  
for e, use formal definitions of  $O$  and  $\Omega$ ;  
you should probably give specific values for the  $c$  and  $n_0$  in the formulas on pages 53-54.  
for  $c$  &  $d$ , you can use the theorem on p 56.
4. 2.2.7a,d (4 points) (proof or disproof of properties using the formal definition)
5. 2.2.10 (6 points) (door in a wall). Show that your algorithm is  $O(N)$ .
6. 2.3.2 (8 points) (big-theta for various summations)
7. 2.3.10 (10 points) (GE Algorithm – yeah, it's a big secret what GE stands for ☺ ) Include a quantitative indication of how much time is gained by removing the glaring inefficiency.