

MA/CSSE 473 – Design and Analysis of Algorithms

Homework 6

45 points total

(Summer: in drop box) These are to be turned in as hard copy. You can write solutions out by hand, or write them on your computer and print them. If there are multiple pages, please staple them together.

When a problem is given by number, it is from the textbook. 1.1.2 means “problem 2 from section 1.1” .

Problems for enlightenment/practice/review (not to turn in, but you should think about them):

How many of them you need to do serious work on depends on you and your background. I do not want to make everyone do one of them for the sake of the (possibly) few who need it. You can hopefully figure out which ones you need to do.

- 4.1.1 (divide-and-conquer array max for unsorted array)
- 4.1.2 (divide-and-conquer array max/min for unsorted array)
- 4.1.7 (Mergesort stability)
- 4.1.9 ($O(n \log n)$ algorithm to count inversions in an array)

Problems to write up and turn in:

1. (3) 4.1.4 (logarithm base in the Master Theorem)
2. (6) 4.1.5 (Simple application of the Master Theorem)
3. (6) (RSA attacks) Read about various ways of attacking the RSA cryptosystem.
Write about two attacks that interest you. Explain how they work.
One place you can look is <http://en.wikipedia.org/wiki/Rsa> ,
4. (15) (Miller-Rabin test) Let $N = 561$. For how many choices of a is $a^{560} \equiv 1 \pmod{561}$? How many of these liars are "outed" by the Miller-Rabin test.? [Hint: writing a few lines of code may help you here].
5. (15) (RSA decoding). If small primes are used, it is computationally easy to "crack" RSA codes.
Suppose my public key is $N=703$, $e= 41$. You intercept an encrypted message intended for me, and the encrypted message is 361. What was the original message?