Sophomore Engineering Curriculum

ES 202

Fluid and Thermal Systems

## **Homework Set #2**

Assignment #1:

Open up your favorite web browser and go to <u>http://web.mit.edu/fluids/www/Shapiro/ncfmf.html</u> Watch the 38-minute video titled "Deformation of Continuous Media" and answer the following questions:

- a) Name four important characteristics of the principal axes.
- b) What does vorticity measure?

## Assignment #2:

(Adapted from R. M. Olson and S. J. Wright, *Essentials of Engineering Fluid Mechanics*, 5<sup>th</sup> edition, Harper & Row, New York, 1990)

Determine if the following velocity fields describe an irrotational fluid flow. Clearly show your logic.

a) 
$$V_x = x^2 \cos(y), \quad V_y = -2x \sin(y)$$

b) 
$$V_x = x + 2$$
,  $V_y = 1 - y$ 

c) 
$$V_x = x y t$$
,  $V_y = x^3 - \frac{y^2 t}{2}$ 

d) 
$$V_x = \ln(x) + y$$
,  $V_y = x y - \frac{y}{x}$ 

e) 
$$V_x = x + y$$
,  $V_y = x - y$ 

## Assignment #3:

The following functions of x and y have been suggested as possible stream functions for a steady, incompressible flow.

a) 
$$\psi_1 = x^2 + 2y$$

b) 
$$\psi_2 = 5 x y$$

In each case,

- i. determine if the flow is rotational or irrotational.
- ii. sketch several streamlines (lines of constant  $\psi$ ) in the *x*-*y* plane (-5 < *x* < 5, 0 < *y* < 5). What steady physical flow would the flow field represent? (Recall that because there is no flow across a streamline, every streamline could represent a solid boundary.)